

**LOCAL-IN-TIME EXISTENCE AND REGULARITY OF
THE n -DIMENSIONAL NAVIER-STOKES EQUATIONS
VIA DISCRETIZATIONS**

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Consider the equations:

$$\begin{aligned}u_t &= \nu \Delta u - (u \cdot \nabla)u - \nabla p + f \\ \operatorname{div} u &= 0\end{aligned}$$

for $x \in [0, 1]^n$ and $t \in (0, \infty)$, together with periodic boundary conditions and initial condition $u(x, 0) = g(x)$ (with $\operatorname{div} g = 0$).

We present a proof of local-in-time existence of a smooth solution based on a discretization by a suitable Euler scheme. It will be shown that this solution exists in an interval $[0, T)$, where T depends on n , f and g . The proof given shows that the local-in-time regularity for this problem can be obtained by simple pointwise estimates of the solutions of the discretized problem.

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